

Problem Solving Models

Understanding Problems

Problem-Solving

Develop problem-solving skills

Organize information

Practice communication skills

Write a solution sentence

Patterns

Communicate problem-solving ideas

Develop problem-solving strategies

Organize information

Expressions and Formulas

Translate verbal sentences into expressions and equations

Use formulas to solve problems

Proportional Reasoning

Use proportional reasoning to solve problems

Write and solve a proportion

Unit Analysis

Apply rates to solve a problem

Use proportions to solve problems

Use unit or dimensional analysis to solve a problem

Functions and Graphs

Understand Functions

Identify functional relationships between two variables

Identify input and output involving two variable quantities

Identify trends in data numerically and graphically

Represent functions between two variables using tables and graphs

Domain and Range

Determine the domain and range of a function

Identify the independent and dependent variables of a function

Write the equation to define a function



Mathematical Modeling

Develop a function model

Identify a mathematical model

Recognize patterns and trends between two variables using tables as models

Solve problems using formulas as a model

Solving an Equation

Solve an equation numerically and graphically

Solve an equation using algebra techniques

Write and Solve Equations

Develop models to solve problems

Solve equations with variables on both sides

Solve formulas for a specified variable

Use the distributive property

Reading Graphs

Describe graphs in words

Identify increasing, decreasing and constant parts of graphs

Identify maximum and minimum of a graph

Sketch a graph to represent a situation

Graphical and Statistical Models

Data Analysis

Misleading Graphs

Recognize scaling of axes on graphs

Scaling axes of graphs

Bar and Circle Graphs

Read and interpret bar graphs

Read and interpret circle graphs

Read tables

Scatterplots

Construct scatterplots

Estimate and draw a best fit line

Estimate errors of line of best fit



Organizing Data

Collect and organize data

Plot data in a scatterplot

Recognize linear patterns in data

Data Distribution

Determine measures of central tendency

Organize data with frequency tables, dotplots, and histograms

Recognize symmetric and skewed frequency distributions

Variability

Measure the variability of frequency distributions

Read and understand box-and-whisker plots

Use standard deviation to understand mean

Probability and Counting Methods

Probability

Determine relative frequency for a set of data

Determine theoretical and experimental probability

Simulate an experiment

Understand properties of probability

Sample Space

Apply the multiplication principle of counting

Determine the sample space for a probability distribution

Display a sample space with a tree diagram

Permutations and Combinations

Determine the number of combinations

Determine the number of permutations

Binomial Probability

Calculate binomial probabilities

Recognize components of binomial experiments

Function Models

Linear Equations

Average Rate of Change

Determine the average rate of change

Understand the use of delta notation



Slope

Determine slope of a line between two points

Identify increasing and decreasing linear functions using slope

Identify linear functions by a constant rate of change

Interpret slope as an average rate of change

Slope-Intercept Form

Develop the slope-intercept model of an equation of a line

Identify situations modeled by an equation

Use intercepts of a graph

Use the slope-intercept formula to determine intercepts

Write Linear Equations using Slope & y-Intercepts

Interpret slopes and y-intercepts

Write an equation for a linear function given its slope and y-intercept

Write linear functions in slope-intercept form

Write Linear Equations using Two Points

Determine the equation using two points

Determine the slope and y-intercept using equations and graphs

Interpret slopes and y-intercepts

Systems of Equations

Interpret the solution to a system of equations

Solve a system of two linear equations

Use the substitution method to solve systems of equations

Break-Even Points

Determine the break-even point of a linear system

Interpret break-even points on a graph

Solve a system of two linear equations

Inequalities and Quadratics

Linear Inequalities

Solve compound inequalities

Solve linear inequalities numerically and graphically

Use properties of inequalities to solve inequalities



Quadratic Functions

Evaluate functions of the form y = ax2

Graph functions of the form y = ax2

Interpret the coordinates of points on the graph $y = ax^2$

Solve an equation of the form ax2 = c using square roots

Quadratic Equations

Explore the role of a, b and c as it relates to the graph of quadratic equation

Identify functions of the form y = ax2+bx+c as quadratic functions

Parabolas

Determine the axis of symmetry of a parabola

Determine the intercepts of a parabola

Determine the vertex of a parabola

Identify the domain and range

Interpret the meaning of the vertex and intercepts of a parabola

Solving Quadratic Equations

Solve quadratic equations graphically

Solve quadratic equations numerically

The Quadratic Formula

Identify solutions of quadratic equations using a graph

Use the quadratic formula to solve quadratic equations

Quadratic Regression Models

Determine quadratic regressions models

Solve problems using quadratic regressions models

Financial Models

Personal Finance

Personal Finances

Solve problems involving personal finances

Interest

Apply the compound interest formula to determine future values of a lump sum investment

Apply the present value formula

Determine effective interest rate

Distinguish between simple and compound interest



Annuities

Determine future and present values using technology

Determine the future value of an ordinary annuity using a formula

Determine the present value of an ordinary annuity

Distinguish between an ordinary and an annuity due

Solving problems involving annuities

Amortization

Determine the amortization payment of a loan using technology

Determine the amortization payment on a loan using a formula

Solve problems involving repaying a loan or liquidating a sum of money by amortization model

Use technology to determine past and present values of annuities

Future Planning Finance

Installment Loans

Determine an installment payment

Determine annual percentage rate (APR) using the APR formula and using a table

Determine interest on a credit card using average daily balance

Determine the amount financed, installment price and finance charges of an installment loan

Determine unearned interest on a loan if prepayment

Mortgages

Determine if borrowers qualify for a mortgage

Determine monthly mortgage payments using a table

Determine the amount of a down payment and points in a mortgage

Determine total interest on mortgages

Prepare a partial amortization schedule of a mortgage

Life Insurance

Calculate the value of each of the nonforfeiture options for a cancelled permanent life insurance policy

Determine the annual life insurance premium for different types of policies using a table

Distinguish between term and permanent life insurance

Stocks and Bonds

Calculate the price of bonds

Distinguish between a stock and a bond

Read stock and bond listings

Solve problems involving stocks and bonds



Exponential, Trigonometric and Variation Models

Exponential Functions

Growth and Decay Factors

Apply growth and decay factors involving percents of increase and decrease

Define growth and decay factors

Determine growth and decay factors from percents of increase and decrease

Consecutive Growth and Decay Factors

Apply consecutive growth and or decay factors involving percent changes

Define consecutive growth and decay factors

Determine a consecutive growth or decay factor from consecutive percent changes

Exponential Functions

Graph exponential functions from data and equations

Graph exponential functions from symbolic rules

Recognize an exponential function as a rule for apply growth or decay factors

Use Exponential Functions

Determine growth and decay factors for exponential functions represented by a table of values or an equation

Determine the doubling and halving time

Graph exponential functions defined by y = abx

Population Growth

Determine annual growth or decay rate of an exponential function represented by a table of values or an equation

Graph an exponential function having equation $y = a(1 \pm r)2$

Equations of Exponential Functions

Determine the equation of an exponential function that best fits the given data

Determine whether a linear or exponential model best fits given data

Make predictions using an exponential regression equation

Trigonometric Functions

Right Triangles

Determine the sine, cosine, and tangent of an acute angle by using technology

Determine the sine, cosine, and tangent of an angle using right triangles

Identify sides and corresponding angles of a right triangle

Use proportions to determine side lengths of similar right triangles

Angle Relationships

Demonstrate that the sine and cosine of complementary angles are equal

Identify complementary angles



Inverse Functions

Determine the inverse sine and cosine of a number using technology

Determine the inverse tangent of a number

The Sine Function

Determine the equation of a sine function that best fits given data

Make predictions using a sine regression equation

The Unit Circle

Determine the coordinates of points on a unit circle using sine and cosine functions

Identify the properties of the graphs of sine and cosine functions

Sketch a graph of $y = \sin x$ and $y = \cos x$

Degree and Radian Measures

Convert between degree and radian measures

Identify the period and frequency of a function defined by y = a sin(bx) or y = a cos(bx) using the graph

Amplitude and Period

Determine the amplitude of the graph of $y = a \sin(bx)$ and $y = a \cos(bx)$ using a formula

Determine the period of the graph of $y = a \sin(bx)$ and $y = a \cos(bx)$ using a formula

Wavelength and Frequency

Determine the sine model for a given frequency

Know the relationship between wavelength and frequency

Variation of Functions

Direct Variation

Determine the constant of proportionality in a direct variation problem

Recognize equivalent forms of the direct variation statement

Solve direct variation problems

Inverse Variation

Graph an inverse variation relationship

Recognize equations of the form xy = k as inverse variations

Recognize functions of the form y = k/x as nonlinear

Solve equations of the form a/x = b

Constant of Variation

Describe the properties of graphs having the equation y = k/x

Determine the constant of variation

Graph an inverse variation function defined by an equation of the form y = k/x



Geometric Models

Plane Figures

Perimeter

Recognize perimeter as a geometric property of plane figures

Use unit analysis to solve problems involving perimeter

Write and use formulas for circumference

Write formulas for and calculate perimeters of plane figures

Perimeter of Composite Figures

Calculate perimeters of many-sided plane figures using combinations of formulas

Use unit analysis to solve problems involving perimeters

Area

Calculate areas of polygons using formulas

Determine the area of a circle by formula

Write formulas for areas of polygons

Area and Perimeter in Context

Distinguish between problems requiring area and perimeter formulas

Solve problems in context using geometric models

Tessellations

Identify a tessellation

Identify reflective and translational symmetry

Perform a glide reflection on a given figure

Perform a transformation on a given figure

Reflect, translate and rotate a given figure

Similar Triangles

Recognize geometric properties of similar triangles

Use similar triangles in indirect measurement

Relationships in Figures

Recognize a golden rectangle by finding the golden ratio

Recognize Fibonacci numbers and the limit of the ratio of successive Fibonacci numbers

Understand Desargue's Theorem

Understand one- and two-point perspective



Three-Dimensional Figures

Surface Area

Recognize properties of three-dimensional figures

Write formulas for and calculate surface area of three-dimensional figures

Volume of Prisms and Cylinders

Recognize geometric properties of three-dimensional figures

Write formulas for and calculate volumes of prisms and cylinders

Volume of Spheres and Cones

Write formulas for and calculate volumes of spheres and cones

Scale Drawings

Use geometry formulas to solve problems

Use scale drawings in the problem-solving process